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REGNO:-TMC -D/79/89/36

CODE:- AG-5-1899 **General Instructions :**

- All question are compulsory. 1.
- 2. The question paper consists of 29 questions divided into three sections A,B and C. Section - A comprises of 10 question of 1 mark each. Section - B comprises of 12 questions of 4 marks each and Section - C comprises of 7 questions of 6 marks each.
- Question numbers 1 to 10 in Section A are multiple choice questions where you are to select one 3. correct option out of the given four.
- There is no overall choice. However, internal choice has been provided in 2 question of four marks and 4. 2 questions of six marks each. You have to attempt only one If the alternatives in all such questions.
- Use of calculator is not permitted. 5.
- Please check that this question paper contains 3 printed pages. 6.
- Code number given on the right hand side of the question paper should be written on the title page of 7. the answer-book by the candidate.

सामान्य निर्देश :

- सभी प्रश्न अनिवार्य हैं। 1.
- इस प्रश्न पत्र में 29 प्रश्न है, जो 3 खण्डों में अ, ब, व स है। खण्ड अ में 10 प्रश्न हैं और प्रत्येक प्रश्न 1 अंक का है। खण्ड ब में 2. 12 प्रश्न हैं और प्रत्येक प्रश्न 4 अंको के हैं। खण्ड – स में 7 प्रश्न हैं और प्रत्येक प्रश्न 6 अंको का है।
- प्रश्न संख्या 1 से 10 बहविकल्पीय प्रश्न हैं। दिए गए चार विकल्पों में से एक सही विकल्प चनें। 3.
- इसमें कोई भी सर्वोपरि विकल्प नहीं है. लेकिन आंतरिक विकल्प 2 प्रश्न 4 अंको में और 2 प्रश्न 6 अंको में दिए गए हैं। आप दिए गए 4. विकल्पों में से एक विकल्प का चयन करें।
- 5. कैलकूलेटर का प्रयोग वर्जित हैं ।

CLASS – XII

- कृपया जाँच कर लें कि इस प्रश्न–पत्र में मुद्रित पृष्ठ 3 हैं। 6.
- प्रश्न–पत्र में दाहिने हाथ की ओर दिए गए कोड नम्बर को छात्र उत्तर–पुस्तिका के मुख–पृष्ठ पर लिखें। 7.

Pre-Board Examination 2010 -11

CBSE

Time: 3 Hours Maximum Marks: 100

Total No. Of Pages :3

अधिकतम समय : 3 अधिकतम अंक : 100

कुल पृष्ठों की संख्या : 3

MATHEMATICS

Section A			
Q.1	Find the maximum and minimum values, if any of $f(x) = \sin 3x - 3$. Ans .max =-2, mini=-3		
Q.2	Find the direction cosines of x-axis. Ans (1,0,0).		
Q.3	If the following matrix is skew symmetric, find the values of a, b, c.If $A = \begin{bmatrix} 0 & a & 3 \\ 2 & b & -1 \\ c & 1 & 0 \end{bmatrix}$. Ans $a = -2, b = 0, c = -3$		
Q.4	Evaluate: $\int (e^x \log a + e^a \log x + e^a \log a) dx$. Ans $\frac{a^x}{\log a} + \frac{x^{a+1}}{a+1} + a^a x + c$		
Q.5	Evaluate : $\int \frac{dx}{x^2 (x^4 + 1)^{3/4}}$. Ans = $-(1 + x^{-4})^{\frac{1}{4}} + c$		
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Q.6	Find the point on the curve $y^2 = 8x$ for which the abscissa and ordinate change at the same rate. Ans
	$\frac{dy}{dx} = 1$ (2,4)
Q.7	Find the inverse element of the binary relation $a \otimes b = a + b - 4$. Ans $e = 4, d = 8-a$ Ans=
Q.8	The slope of tangent to curve $y = \frac{x-1}{x-2}atx = 10$. Ans $\frac{dy}{dx} = -\frac{1}{64}$
Q.9	If $A^2 = A$ for $A = \begin{bmatrix} -1 & b \\ -b & 2 \end{bmatrix}$, then find the value of b. Ans $b = \pm \sqrt{2}$
Q.10	Find the value of $\sec^2(\tan^{-1}2)$. Ans =5
	Section B
Q.11	Define a binary operation * on the set {0, 1, 2, 3, 4, 5} as $a * b = \begin{cases} a + b, & \text{if } a + b < 6 \\ a + b - 6, & \text{if } a + b \ge 6 \end{cases}$
	Show that zero is the identity for this operation and each element <i>a</i> of the set is invertible with $6 - a$ being the inverse of <i>a</i> .
Q.12	It is given that for the function f given by $f(x) = x^3 + bx^2 + ax$, $x \in [1,3]$ Rolle's theorem holds with
	$c = 2 + \frac{1}{\sqrt{3}}$. Find the values of a and b. Ans $a = 11$; $b = -6$
Q.13	Prove that $\begin{vmatrix} a & b & c \\ a-b & b-c & c-a \\ b+c & c+a & a+b \end{vmatrix} = a^3 + b^3 + c^3 - 3abc$. Also prove that value of determinant is always
	positive if a, b, c is positive real number.
Q.14	Evaluate : $\int_{0}^{1} \sin^{-1} \left(x \sqrt{1-x} - \sqrt{x} \sqrt{1-x^2} \right) dx, 0 \le x \le 1$. Ans $= \frac{\pi}{4} - 1$
	OR
	Evaluate: $\int_{0}^{\pi/2} \sin 2x \tan^{-1}(\sin x) dx$. Ans $=\frac{\pi}{2} - 1$
Q.15	Find all the points of discontinuity of the function $f(x) = [x^2]$ on $[1, 2)$ where $[]$ denotes the greates
	$\begin{bmatrix} 1 & ; & x \in [1, \sqrt{2}) \end{bmatrix}$
	integer function. Ans f (x) = $\begin{cases} 2 & ; x \in [\sqrt{2}, \sqrt{3}) \\ 3 & ; x \in [\sqrt{3}, 2) \end{cases}$ at x = $\sqrt{2}$; RHL = 2 & LHL = 1 \therefore RHL \neq LHL a
	$=\sqrt{3}$; RHL = 3 & LHL = 2 : RHL \neq LHL there fore poit of discontinuity $\sqrt{2}$ & $\sqrt{3}$ on [1, 2]
Q.16	Find the particular solution of the differential equation
	$(xdy - ydx)y.\sin\left(\frac{y}{x}\right) = (ydx + xdy)x\cos\frac{y}{x}$, given that $y = \pi$ when x=3. Ans $\sec\frac{y}{x} = \frac{2xy}{3\pi}$
Q.17	Solve the differential equation: $\frac{d^2 x}{dy^2} = y \sin^2 y$ Ans $x = \frac{y^3}{12} + \frac{y}{8} \cos 2y - \frac{\sin 2y}{8}$
	OR Example a differential equation of the summer $A x^{x} + B x^{-x} + x^{2}$. A and B are arbitrary constants. An
	Form a differential equation of the curve $xy = Ae^{-1} + Be^{-1} + x^{-1}$, A and B are arbitrary constants. Any $d^2y = dy$
	$x\frac{d^2y}{dx^2} + 2\frac{dy}{dx} = xy - x^2 + 2$
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Q.18	An urn contains 25 balls of which 10 balls bear a mark 'X' and the remaining 15 bear mark 'Y'. A ball is drawn at random from the urn, its mark is noted down and it is replaced. If 6 balls are drawn in this way, find the probability that (i) all will bear 'X' mark. (ii) not more than 2 will bear 'Y' mark (iii) at least one ball will bear 'Y' mark	
	(iv) the number of balls with 'X' mark and 'Y' mark will be equal . Ans (i) $\frac{64}{15625}$ (ii) $\frac{2796}{15625}$	
	$\frac{(iii)\frac{15501}{15625}(iv)\frac{001}{3125}}{OR}$	
	In a hurdle race, a player has to cross 10 hurdles. The probability that he will clear each hurdle is 5 /	
	6. What is the probability that he will knock down fewer than 2 hurdles? Ans $\frac{5^9 \times 15}{6^{10}} = \frac{5^{10}}{6^{10}} \times 3$	
Q.19	If $\vec{a} \times \vec{b} = \vec{c} \times \vec{d}$ and $\vec{a} \times \vec{c} = \vec{b} \times \vec{d}$, show that $\vec{a} - \vec{d}$ is parallel to $\vec{b} - \vec{c}$ where $\vec{a} \neq \vec{d} \& \vec{b} \neq \vec{c}$.	
Q.20	If $y = \cot^{-1}(\sqrt{\cos x}) - \tan^{-1}(\sqrt{\cos x})$ Prove that $\sin y = \tan^2 \frac{x}{2}$.	
Q.21	If $y = (x + \sqrt{x^2 + 1})^m$, then show that $(x^2 + 1)\frac{d^2y}{dx^2} + x\frac{dy}{dx} - m^2y = 0$.	
	OR	
	If $y = x^{-1}$ then prove that $\frac{d^{-1}y}{dx^{-2}} - \frac{1}{y} \left(\frac{dy}{dx}\right) - \frac{y}{x} = 0$.	
Q.22	Find the vector equation of the line parallel to the line $\frac{x-1}{2} = \frac{2-y}{-3} = \frac{z-3}{4}$ and passing through the	
	point (2, 4, 5). Also find the distance between two lines. Ans $\vec{r} = (2i+4j+5k) + \lambda(2i+3j+4k)$	
	S.D. = $\frac{\left \left(\vec{a}_2 - \vec{a}_1 \right) \times \vec{b} \right }{\left \vec{b} \right } = \frac{\sqrt{5}}{\sqrt{29}} \& \left(\vec{a}_2 - \vec{a}_1 \right) \times \vec{b} = 2i - k$	
	Section C	
Q.23	$If_{A} = \begin{bmatrix} 2 & 3 & 4 \\ 5 & 4 & -6 \\ 3 & -2 & -2 \end{bmatrix} and_{B} = \begin{bmatrix} 20 & 2 & 34 \\ 8 & 16 & -32 \\ 22 & -13 & 7 \end{bmatrix} are two square matrices, find AB and hence Solve the$	
	system of linear equation : $\frac{2}{x} + \frac{3}{y} + \frac{4}{z} = -3;; \frac{5}{x} + \frac{4}{y} - \frac{6}{z} = 4; \frac{3}{x} - \frac{2}{y} - \frac{2}{z} = 6$. Ans $\begin{bmatrix} 1\\ -1\\ -2 \end{bmatrix}$	
Q.24	Evaluate : $\int \frac{1}{\sin x(5-4\cos x)} dx$. Ans. $\frac{1}{2} \log(1-\cos x) - \frac{1}{18} \log(1+\cos x) - \frac{4}{9} \log((5-4\cos x))$	
Q.25	Two bag A and B contains 4 white and 3 black balls and 2 white and 2 black balls respectively. From bag A, two balls are drawn at random and then transferred to bag B. A ball is then drawn from bag B and is found to be a black ball. What is the probability that the transferred balls were 1 white and 1	
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	black? Ans Required Probability = $\frac{\frac{24}{42} \times \frac{3}{6}}{\frac{12}{42} \times \frac{2}{6} + \frac{6}{42} \times \frac{4}{6} + \frac{24}{42} \times \frac{3}{6}} = \frac{3}{5}$
Q.26	Draw the rough sketch of the region enclosed between the circles $x^2 + y^2 = 4$ and $(x-2)^2 + y^2 = 1$. Using integration, find the area of the enclosed region . Ans Required Area = $2\left\{\int_{1}^{7/4} \sqrt{1-(x-2)^2} dx + \int_{7/4}^{2} \sqrt{4-x^2} dx\right\} = \frac{5\pi}{2} - \frac{\sqrt{15}}{2} - \sin^{-1}\left(\frac{1}{4}\right) - 4\sin^{-1}\left(\frac{7}{8}\right)$ sq. unit OR Prove that the curves $y^2 = 4x \& x^2 = 4y$ divide the area of square bounded by $x = 0$, $x = 4$, $y = 4$ and
Q.27	y = 0 into three equal parts. Ans $A_1 = \int_0^1 (x - \sqrt{4x}) dx = A_2 = \int_0^1 (\sqrt{4x} - \frac{1}{4}) dx = A_3 = \int_0^1 (\frac{1}{4}) dx = \frac{1}{3}$ A toy company manufactures two types of dolls, A & B. Market tests and available recourses have indicated that the combined production level should not exceeds 1200 dolls per week and the demand for dolls of type B is at most half of that for doll of type A. Further the production level of dolls of type A can exceeds three times the production of dolls of other type by at most 600 units. If the company makes profit of $\overline{\xi}$ 12 and $\overline{\xi}$ 16 per doll respectively on doll A and B ,how many each should be produce weekly in order to maximum profit? Ans: $x \ge 0; y \ge 0; x + y \le 1200; y \le \frac{x}{2}; x \le 3y + 600; P = 12, x + 16, y$ CORNER POINTS : (0,0); (600, 0) (1050, 150); (800, 400) Z is maximum at (800, 400). there fore 800 of type A and 400 of type B should be produce to get maximum profit
Q.28	Find the vector and Cartesian equation of the plane containing the two lines $\vec{r} = 2i + j - 3k + \lambda(i + 2j + 5k)$; $\vec{r} = 2i + j - 3k + \mu(3i - 2j + 5k)$. Also find the inclination of this plane with the XZ plane. Ans $\theta = \cos^{-1}\left(\frac{5}{\sqrt{141}}\right)$ eq $10x + 5y - 4z = 37$
Q.29	A tank with rectangular base and rectangular sides, open at the top is to be constructed so that its depth is 2 m and volume is 8 m3. If building of tank costs ₹ 70 per sq meters for the base and ₹ 45 per square meter for sides. What is the cost of least expensive tank? Ans : $L = x \& B = y$ $xy = 4 : \cos t = l \times b + 2 \times h(l + b) \times 45$ $f(x) = 70 xy + 2 \times 2 \times (x + y) \times 45 = 280 + 180 x + \frac{720}{x} \Rightarrow f'(x) = 0 \Rightarrow x = 2$ Expension 1000
	Expansion 1000 OR A helicopter is flying along the curve $y = x^2 + 2$. A soldier is placed at the point (3, 2). Find the nearest distance between the soldier and the helicopter. Ans $f(x) = (x - 3)^2 + x^4 \Rightarrow (1,3) \& D = \sqrt{5}$
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